

$F_{C_3H_6O}$: 2754 ^{kg/hr}, sat. liq., 1 atm
 F_w : B ^{kg/hr}, 45 °C, 1 atm
 goal. 0.995 $C_3H_8O_2$

Problem 01. "Find k and E_a"

2nd PFR sets were used; SS 1" with Sch. 40, 4^m long, $\frac{H_2O \ C_3H_6O \ \text{mass}}{(0.5-0.5) \ \text{weight}}$, $T_1 = 50^\circ C$ | $x_1 = 0.05$
 $T_2 = 60^\circ C$ | $x_2 = 0.06$
 $P = 1 \ \text{atm}$, $u = 2 \ \text{m/s}$, $k = k_0 \cdot \exp(-\frac{E_a}{RT})$

Nominal pipe size = 1" (outside diameter = 1.315" in), Schedule no. = 40, wall thickness = 0.133" in
 inside diameter = 1.049" in, cross-sectional area of metal = 0.494 in², inside sectional area = 0.006 ft²
 circumference = 0.349 ft of length (outside) = 0.275 ft of length (inside), capacity at 1 ft/s $\rho = 1345 \ \text{lb/hr water}$
 pipe weigh = 1.68 lb/ft

Basis: 1000 gr of the mixture feed
 → 500 gr H₂O $\frac{1 \ \text{mol}}{18.015 \ \text{g}} = 27.755 \ \text{mol H}_2\text{O}$
 → 500 gr C₃H₆O $\frac{1 \ \text{mol}}{58.080 \ \text{g}} = 8.609 \ \text{mol C}_3\text{H}_6\text{O}$ → Limiting component

Stoichiometry table:

Comp.	N ₀ (mol)	x _A N _{A0}	N	w
A (C ₃ H ₆ O)	27.755 8.609	-0.43045	8.179	475.036
B (H ₂ O)	27.755	-0.43045	27.325	492.260
C (C ₃ H ₈ O ₂)	0	+0.43045	0.43	32.721 → 32.704

Σ w_i = 1000 (constraint)

$\ln \frac{C_B \cdot C_{A0}}{C_{B0} \cdot C_A} = (C_{B0} - C_{A0}) kt$

(Case II.)
 $x_A = 0.06$

	N ₀	x _A N _{A0}	N	w
A	8.609	-0.516	8.093	470.091
B	27.755	-0.516	27.239	490.712
C	0	+0.516	0.516	39.266 → 39.247

$$\ln \frac{C_B \cdot C_{A0}}{C_{A0} \cdot C_B} = (C_{B0} - C_{A0})kt \Rightarrow \ln \frac{N_B \cdot N_{A0}}{N_A \cdot N_{B0}} = \frac{(N_{B0} - N_{A0})}{V} kt$$

For case I & II $t_1 = t_2, V_1 = V_2$

$$\left[\frac{\ln \left(\frac{N_B \cdot N_{A0}}{N_A \cdot N_{B0}} \right)}{(N_{B0} - N_{A0})k} \right]_{\text{case I}} = \left[\frac{\ln \left(\frac{N_B \cdot N_{A0}}{N_A \cdot N_{B0}} \right)}{(N_{B0} - N_{A0})k} \right]_{\text{case II}} \quad \text{(I)}$$

$$k = k_0 \cdot \exp\left(\frac{-E_a}{RT}\right)$$

$$\left[\frac{\ln \left(\frac{N_B \cdot N_{A0}}{N_A \cdot N_{B0}} \right)}{(N_{B0} - N_{A0}) \cdot k_0 \cdot \exp\left(\frac{-E_a}{RT}\right)} \right]_{\text{case I}} = \left[\frac{\ln \left(\frac{N_B \cdot N_{A0}}{N_A \cdot N_{B0}} \right)}{(N_{B0} - N_{A0}) \cdot k_0 \cdot \exp\left(\frac{-E_a}{RT}\right)} \right]_{\text{case II}} \quad \text{(II)}$$

substitution

$$\ln \left(\frac{27.325 \times 8.609}{8.179 \times 27.755} \right) = \ln \left(\frac{27.239 \times 8.609}{8.093 \times 27.755} \right)$$

$$(27.755 - 8.609) k_0 \cdot \exp\left(\frac{-E_a}{82.06 \times 10^{-6} \frac{\text{m}^3 \text{atm}}{\text{mol} \cdot \text{K}} \times 323.15}\right) = (27.755 - 8.609) k_0 \cdot \exp\left(\frac{-E_a}{82.10 \times 10^{-6} \times 323.15}\right)$$

$$\Rightarrow 0.0356 \cdot \exp\left(\frac{E_a}{82.0265}\right) = 0.0430 \cdot \exp\left(\frac{E_a}{0.0273}\right) \Rightarrow 1.208 = \exp\left(\frac{E_a}{0.0265} - \frac{E_a}{0.0273}\right)$$

$$\ln \Rightarrow 0.189 = \frac{0.0008 E_a}{7.2345 \times 10^{-4}} \Rightarrow E_a = 0.1709 \frac{\text{m}^3 \text{atm}}{\text{mol}} \times \frac{101392}{1 \text{ atm}} = 17329.42 \frac{\text{J}}{\text{mol}}$$

$$V = \frac{\pi d_{in}^2 L}{4} = \frac{\pi (1.049 \text{ in} \times 0.0254 \frac{\text{m}}{\text{in}})^2 \times 9 \text{ m}}{4} = 0.00223 \text{ m}^3$$

$$u = 2 \text{ m/s} \Rightarrow u = \frac{L}{t} \Rightarrow t = \frac{V}{u} = \frac{0.00223 \text{ m}^3}{2 \text{ m/s}} = 0.001115 \text{ s}$$

$$\text{(I)} \Rightarrow \left[\frac{\ln \left(\frac{N_B \cdot N_{A0}}{N_A \cdot N_{B0}} \right)}{(N_{B0} - N_{A0}) k_0 \cdot \exp\left(\frac{-E_a}{RT}\right)} \right]_{\text{case I}} = \frac{t}{V} \Rightarrow \frac{0.0356 \cdot \exp\left(\frac{0.1709}{0.0265}\right)}{19.196 k_0 \cdot} = \frac{0.001115 \text{ s}}{0.00223}$$

$$\Rightarrow \frac{1.1753}{k_0} = 0.2491 \Rightarrow k_0 = 4.7182 \frac{\text{m}^3}{\text{mol} \cdot \text{hr}}$$

$A = 1.7 \text{ eB}$

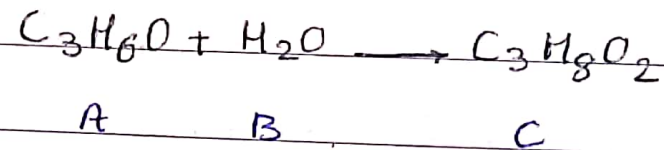
$E_a = 3.24 \text{ eA btu/lbmol}$

Problem 02. what is the mass flow rate of water, B?

$$\begin{array}{l} \text{Basis} = 1 \text{ hr} \\ \rightarrow \text{C}_3\text{H}_6\text{O} = 2759 \frac{\text{kg}}{\text{hr}} \times \frac{1 \text{ kmol}}{58.08 \text{ kg}} = 47.417 \text{ kmol C}_3\text{H}_6\text{O} \\ \rightarrow \text{H}_2\text{O} = B \frac{\text{kg}}{\text{hr}} \times \frac{1 \text{ kmol}}{18.015 \text{ kg}} = \frac{B}{18.015} \text{ kmol H}_2\text{O} \end{array}$$

for $\text{C}_3\text{H}_6\text{O}$ to be the limiting component, there should be: $\frac{B}{18.015} > 47.417 \Rightarrow B > \underline{854.217 \text{ kg}}$

Problem 03. Compute Equilibrium constant of the reaction.



Due to the given rate of reaction, $(-r_A = k_f C_A C_B)$

there is no reverse path for reaction to take place. Thus: $k_{eq} = \frac{k_f}{k_b} = \infty$